

COMPUTER PROJECT 2

Space Curves, Arc Length, and Curvature

Instructions: Use *Mathematica* to solve the following problems. Be sure to clearly label each section of your notebook based on which problem you are solving. You can change an input cell to a text cell by selection the Format tab from the top menu and choosing Text from the Style option. Email a copy of your finalized notebook to byoung@wyomingseminary.org with the subject "Computer Project 2."

For this project, you will be given a periodic space curve (with period 2π), $\vec{r}(t)$. The curve is different for each student and can be found on the next page.

- 1) Use the `ParametricPlot3D` command to generate a plot of the space curve for $0 \leq t \leq 2\pi$.
- 2) Use the `ArcLength` command to numerically compute the arc length of the curve over the interval $0 \leq t \leq 2\pi$. Make sure your answer is accurate to at least 3 decimal places. You will need to pass the option `WorkingPrecision` \rightarrow 10 to the `ArcLength` command.
- 3) Use *Mathematica* to give a plot of the curvature of your space curve as a function of t over $0 \leq t \leq 2\pi$. You can use the command `ArcCurvature` to compute the function.
- 4) Use the command `FindMaximum` to identify the point of maximum curvature. Give a second plot of the space curve where you explicitly mark this point.

Student Data

Student	Space Curve
Yang Cao	$\langle 4 \sin^2(2t) + 2 \cos(3t), 2 \sin(2t) + 6 \cos^2(3t), \sin^2(t) + 6 \sin(2t) \cos(3t) \rangle$
Abigail Ryu	$\langle 6 \sin^2(4t) + 5 \cos(3t), 5 \sin(4t) + 5 \cos^2(3t), \sin^3(t) + 6 \sin(4t) \cos(3t) \rangle$
Andrew Tsui	$\langle 6 \sin^2(4t) + 5 \cos(5t), 5 \sin(4t) + 6 \cos^2(5t), \sin^3(t) + 4 \sin(4t) \cos(5t) \rangle$
Theo Yang	$\langle 6 \sin^2(4t) + 4 \cos(3t), 4 \sin(4t) + 3 \cos^2(3t), \sin^3(t) + 6 \sin(4t) \cos(3t) \rangle$